THE ORIGIN OF PROLATE ROTATION IN DWARF SPHEROIDAL GALAXIES FORMED BY MERGERS OF DISKY DWARFS

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ABSTRACT

Motivated by the discovery of prolate rotation of stars in Andromeda II, a dwarf spheroidal companion of M31, we study its origin via mergers of disky dwarf galaxies. We simulate merger events between two identical dwarfs changing the initial inclination of their disks with respect to the orbit and the amount of orbital angular momentum. On radial orbits the amount of prolate rotation in the merger remnants correlates strongly with the inclination of the disks and is well understood as due to the conservation of the angular momentum component of the disks along the merger axis. For non-radial orbits prolate rotation may still be produced if the orbital angular momentum is initially not much larger than the intrinsic angular momentum of the disks. The orbital structure of the remnants with significant rotation is dominated by box orbits in the center and long-axis tubes in the outer parts. The frequency analysis of stellar orbits in the plane perpendicular to the major axis reveals the presence of two families roughly corresponding to inner and outer long-axis tubes. The fraction of inner tubes is largest in the remnant forming from disks oriented most vertically initially and is responsible for the boxy shape of the galaxy. We conclude that prolate rotation results from mergers with a variety of initial conditions and no fine tuning is necessary to reproduce this feature.

We compare the properties of our merger remnants to those of dwarfs resulting from the tidal stirring scenario and the data for Andromeda II.

Subject headings: galaxies: dwarf – galaxies: Local Group – galaxies: fundamental parameters – galaxies: kinematics and dynamics – galaxies: structure

1. INTRODUCTION

The most widely recognized theory of structure formation in the Universe is based on the assumption of the existence of cold dark matter, significantly dominating the baryonic one. In such a Universe, galaxies form by hierarchical merging of smaller systems. Large galaxies show plenty of signs of past or ongoing mergers but it seems harder to collect observational evidence on the mass scale of dwarf galaxies. Nevertheless, some serious effort has already been made in order to reveal signs of galactic mergers down to $\sim 10^8 M_{\odot}$ (Geha et al. 2005; Martinez-Delgado et al. 2012; Crnojević et al. 2014; Paudel et al. 2015).

In parallel, attempts have been made to understand dwarf mergers from the point of view of numerical simulations. In this case high resolution is needed in order to adequately model a low-mass galactic merger in a cosmological context because of the differences in scales. Although limited in resolution, studies in the context of the Local Group demonstrated that a significant fraction of present-day dwarfs underwent a significant merger with another dwarf galaxy in the past (Klimentowski et al. 2010; Deason et al. 2014). These mergers most likely occur early on, at the outskirts of the Local Group and between bound pairs or within groups. Kazantzidis et al. (2011) demonstrated that mergers between initially disky dwarf galaxies may produce pressure-supported systems with parameters very similar to those of dwarf spheroidal (dSph) galaxies found in the Local Group. These systems seem particularly suitable for testing the merger paradigm on small scales as their proximity offers a possibility for high-resolution measurements.

A few candidates for merger remnants have been already identified among the dSph galaxies of the Local Group. The first was the Fornax dwarf for which shells of stars in the vicinity of the main body were observed (Coleman et al. 2005). Other cases may include the most distant dSphs such as Cetus and Tucana that could not have interacted with the Milky Way and M31 very strongly in the past and be tidally transformed so the merger scenario seems particularly plausible (Kazantzidis et al. 2011), though hypothetical as no direct observational evidence exists in this case.

Recently, a new merger candidate appeared in the form of the Andromeda II (And II) dSph galaxy, one of the brightest satellites of M31. The object has a number of peculiar features. Ho et al. (2012) detected strong rotation signal along the 2D minor axis which means that the object probably has a streaming motion around the longest axis in 3D, i.e. prolate rotation. Note that And II is the only dSph with a clear prolate rotation reported so far. McConnachie et al. (2007) identified a few distinct stellar populations in And II differing in age, metallicity and density profiles. However, Ho et al. (2012) found no significant difference in the kinematics of the metal rich and metal poor stars. The presence of the metallicity gradient was recently confirmed by Ho et al. (2013) and Vargas et al. (2014). Vargas et al. (2014) also found an intermediate age population which makes And II an exception among their sample of six fainter dSphs that possess only populations of stars older than 10 Gyr. Moreover, Amorisco et al. (2014) reported the detection of re-
regions with lower velocity dispersion in the kinematic data of Ho et al. (2012) which can be interpreted as a presence of a stellar stream in And II. Lokas et al. (2014a) proposed a merger scenario for the origin of And II. In this model, the merger occurs between two dwarf galaxies initially composed of a disk and a dark matter halo. The dwarfs had equal masses and only differed by the disk scale lengths. They were placed on a radial orbit towards each other and their disks were inclined by ±45 deg to the collision axis so that the angular momentum vectors of the disks and the velocities of the dwarfs were initially in the same plane. The model adequately reproduces the observed properties of And II, including the prolate rotation and shape. The presence of the different stellar populations can be interpreted as originating from different dwarfs: the two populations then have different density distributions (as a result of different initial disk scale lengths) but very similar kinematics.

Another scenario known to lead to the formation of dSph galaxies is the one based on tidal interaction of the initially disky dwarf satellites with bigger hosts, like the Milky Way or M31 (e.g. Lokas et al. 2014a, 2015). However, as argued by Lokas et al. (2014a), tidal interaction is able to remove very efficiently the initial rotation of the disk (around the shortest axis) as it transforms to a bar and then a spheroid, but cannot induce any significant prolate rotation (around the longest axis).

The initial conditions used in the simulation described in Lokas et al. (2014a) may seem rather special making the merger highly improbable. In this paper we aim to investigate how much these conditions may be relaxed and still reproduce the prolate rotation in the final product of the merger. We study the effect of different initial inclination angles of the dwarf disks and the effect of non-radial orbits of the dwarfs. In section 2 we present the simulations used in this study. The orbital evolution of the dwarfs is described in section 3 while their shapes and kinematics in section 4. Section 5 is devoted to a more detailed study of the orbital structure of the remnants. In section 6 we compare the predictions of the scenario based on mergers with an alternative way to form dSph galaxies that relies on their interaction with a bigger host. In section 7 we compare our predictions to the real data for And II and remark on the possible future, more complete model that will describe all the available data. The summary and concluding remarks follow in section 8.

2. SIMULATIONS

We performed five collisionless simulations of mergers between two identical dwarf galaxies. The simulations differed in the initial inclinations of the disks in the dwarfs and their relative velocities. The numerical realization of the dwarf galaxy is the same as used previously in simulations of tidal stirring by Lokas et al. (2014b) and Lokas et al. (2015). The model was generated following the method described in Widrow & Dubinski (2005) and Widrow et al. (2008) which allows to create self-consistent, equilibrium N-body models of galaxies with an exponential disk and an NFW halo (Navarro et al. 1997).

Our dwarf galaxy had a dark matter component in the form of the NFW halo of total mass \(M_h = 10^9 \, M_\odot\) and concentration parameter \(c = 20\). The exponential disk had the mass of \(M_d = 2 \times 10^8 \, M_\odot\), the scale-length \(R_d = 0.41\) kpc and thickness \(z_d/R_d = 0.2\). Each component of the dwarf contained \(10^6\) particles (which makes the total of \(4 \times 10^6\) particles per simulation). The mergers were followed using the N-body simulation code GADGET-2 (Springel 2005) with the adopted softening scale lengths of 0.02 kpc and 0.06 kpc for the disk and halo particles, respectively. Each merger was evolved for 10 Gyr with positions and velocities of the particles stored every 0.05 Gyr.

We chose the coordinate system of the simulation box so that its origin was at the center of gravity of the two dwarfs. Dwarf 1 was always placed at coordinates \((X_1, Y_1, Z_1) = (25, 0, 0)\) kpc and Dwarf 2 at \((25, 0, 0)\) kpc. For radial mergers \(X\) is the original collision axis, for the other ones \(X'\) is the original collision plane. In order to investigate the effects of different disk inclinations and merger orbits, we keep the same model of mass distribution for both dwarfs in all simulations. We also keep the same initial distances, 50 kpc, and the same relative velocity in the direction of the \(X\) axis, 16 km s\(^{-1}\). At the beginning of each simulation, the angular momentum vectors of the dwarf disks lie in the \(XZ\) plane. Of course, introduce a third component of the angular momentum vectors.

### Table 1: Initial Conditions for the Simulations

<table>
<thead>
<tr>
<th>Merger</th>
<th>(V_X)</th>
<th>(V_Y)</th>
<th>(V_Z)</th>
<th>(L_X/L_{tot})</th>
<th>(L_Y/L_{tot})</th>
<th>(L_Z/L_{tot})</th>
<th>Line type</th>
</tr>
</thead>
<tbody>
<tr>
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<td>0.0</td>
<td>0.0</td>
<td>0.71</td>
<td>0.0</td>
<td>0.71</td>
<td>red solid</td>
</tr>
<tr>
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<td>0.0</td>
<td>0.0</td>
<td>0.71</td>
<td>0.0</td>
<td>0.71</td>
<td>red dashed</td>
</tr>
<tr>
<td>I20R</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.71</td>
<td>0.0</td>
<td>0.71</td>
<td>cyan solid</td>
</tr>
<tr>
<td>I90VY1</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.71</td>
<td>0.0</td>
<td>0.71</td>
<td>green solid</td>
</tr>
<tr>
<td>I90VY2</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.71</td>
<td>0.0</td>
<td>0.71</td>
<td>blue solid</td>
</tr>
</tbody>
</table>

Note: Odd rows list the initial conditions for Dwarf 1 and even rows for Dwarf 2 of a given merger. The first column identifies the merger simulation (see text for details). The following columns list the initial components of orbital velocities and angular momenta (in units of the total angular momentum of each dwarf). The last column indicates the type and color of the line used for a given dwarf and simulation in the figures throughout the paper.
due to the finite precision of the computation, the dwarfs can slightly deviate from a given axis or plane during the simulations.

The components of the initial angular momenta of the dwarf disks and the relative initial velocities of the dwarfs for all five simulations are listed in Table 1. The labels assigned to the simulations (the first column of the Table) refer to the starting configuration: the number after ‘I’ stands for the inclination angle (in degrees) between the angular momentum vectors of the dwarfs, ‘R’ means radial merger, and for non-radial mergers ‘VY’ indicates the velocity (in km s\(^{-1}\)) along the Y axis.

We use capital letters to denote relative velocities or distances of the two dwarfs in the simulation as well as the original coordinate system we defined for the simulation (X, Y, Z). Small letters (x, y, z) refer to the coordinate system associated with the principal axes of the components representing the luminous matter of either individual dwarfs (Dwarf 1 or Dwarf 2) or of the whole galaxy resulting from the merger (i.e. disk components of both dwarfs combined). In the latter system the major axis corresponds to the x axis, the intermediate one to y and the minor one to z. Similarly, other quantities related to this system are marked with small letters, e.g. \( v_x \) is the rotation around the major axis of the respective dwarf or galaxy, and such quantities always refer to just the luminous matter.

For comparisons of the results we divide the simulations into two groups: (1) radial merger simulations with different initial inclinations of the disks (I90R, I60R and I120R) and (2) simulations with the same initial inclination but with different initial relative velocities (I90R, I90VY1 and I90VY2). The simulation I90R is included in both groups for reference and is treated as default. This simulation is closest to the one discussed by Lokas et al. (2014a) and shown to reproduce well the properties of And II, except for the fact the we now use identical dwarf progenitors.

3. ORBITS OF MERGING DWARFS

Fig. 1.— Relative distances (top panel) and velocities (bottom panel) of the dwarfs for simulations with different initial relative velocities.

Fig. 2.— Trajectories of dwarfs in simulations with different initial relative velocities.

Fig. 1 shows the evolution of relative distances and velocities of the dwarfs for simulations with different initial relative velocities. For these simulations, the trajectories of the dwarfs in the collision plane (the XY plane) are displayed in Fig. 2. For our radial mergers (along the X axis), the orbits are almost the same in all three cases.

In the case of radial mergers the initial conditions and the subsequent evolution are very symmetrical. As a result, the major axis of the merger remnant is aligned with the merger axis (the X axis of the simulation box). By introducing some velocity in the Y direction (for simulations I90VY1 and I90VY2) we introduce asymmetry in our simulations because the merger becomes prograde for Dwarf 1 and retrograde for Dwarf 2. This causes differences in the properties of the two dwarfs at the end of the simulation for non-radial mergers. All dwarfs initially have the velocity of 8 km s\(^{-1}\) towards the common center of mass. Simulations I90VY1 and I90VY2 have additional 1 km s\(^{-1}\) and 2 km s\(^{-1}\), respectively, in the perpendicular (Y) direction. The second approach of the dwarfs is on a close-to-radial orbit in both cases but for I90VY2 it takes about 0.7 Gyr longer to reach it.

For I90VY1 the merging times and results are quite similar to simulation I90R, although there is less rotation in the final product. The major axis of the merger remnant is in the XY plane but inclined by about 22 deg with respect to the X axis. For I90VY2 the major axis of the remnant also stays in the XY plane, now inclined by 67 deg to the X axis, but otherwise the simulation outcome is very different. There is just a little rotation in the final product and there are significant differences in the shape and rotation between Dwarf 1 and Dwarf 2 at a given time step. For this reason, in the following figures showing the properties of the dwarfs, we plot just the results for Dwarf 1 except for simulation I90VY2 for which we show results for Dwarf 2 as well (the blue dashed curves).

Fig. 3 shows several snapshots from each of the simulations with different initial relative velocities. The dwarfs...
are shown in projection onto the orbital plane XY and the colors code the mean line-of-sight velocity. The first panel of each row shows the situation around the first pericenter passage. We note that Dwarf 1 of I90VY2 (on the right side of the panel) is notably more deformed than Dwarf 2. In the second-column panels dwarfs are located near their first apocenters and the third-column snapshots roughly correspond to the time when the centers of the dwarfs have just merged, but the merger remnant is still far from equilibrium. The last-column panels are the final snapshots from the simulations, after 10 Gyr of evolution.

4. KINEMATICS AND SHAPE

4.1. Prolate rotation

In order to check how much prolate rotation is present in each merger remnant, we found the principal axes of the stellar component of each dwarf separately and computed the mean rotation velocity around the major axis in the sphere of radius 2 kpc centered on the center of the respective dwarf. We plot the evolution of this rotation in time for Dwarf 1 for all simulations in Fig. 4. Due to the symmetry of the initial conditions in radial mergers, the evolution of this rotation in Dwarf 1 is the same as for Dwarf 2 in the same simulation. For I90VY1, the asymmetry is too small to lead to significant differences between the two dwarfs. On the other hand, in the case of I90VY2 the evolution is dramatically different for the two dwarfs, so we include the result for Dwarf 2 as a dashed curve in Fig. 4.

For all simulations, there is essentially no rotation around the intermediate axis and the evolution of the rotation around the minor axis is trivial: the disk preserves the rotation until the two dwarfs actually start to merge and then the rotation vanishes and remains close to zero until the end of the simulation. We show one example of the evolution of the mean rotation velocity around all principal axes for our default simulation I90R in Fig. 5.

Fig. 6 shows the maps of line-of-sight properties of the final outputs for all five simulations in projection onto the xy plane, i.e. as seen along the z axis of the merger remnant. Here, x, y and z correspond to the major, intermediate and minor axis of the combined stellar components of both dwarfs. The images confirm that the rotation signal (middle-column panels of Fig. 6) is around
the longest ($z$) axis, i.e. the rotation is clearly prolate in all simulations, even when the rotation level is very low as in I90VY2.

The amount of prolate rotation in the final product of a given simulation seems to be controlled in a simple way. For radial mergers, decreasing the initial angle between the angular momenta of the dwarfs and the merger axis (which corresponds to decreasing the angle between the angular momenta of the two dwarfs, from 120 to 90 and 60 deg) we get more rotation in the final result. When the initial angular momenta of the disks are more aligned with the merger axis the components of the momenta along the merger axis are larger. Since these components are preserved during such symmetrical mergers the final products have more prolate rotation.

For non-radial mergers, the more orbital velocity we add in the direction perpendicular to the radial, the less intrinsic rotation we get. This result can be interpreted by comparing the orbital and angular momenta of the dwarfs. In the case of I90VY1 (I90VY2) the orbital angular momentum of each dwarf is about twice (four times) larger than the intrinsic angular momentum of the stellar component of the dwarf. We conclude that the prolate rotation in the remnant cannot be produced

if the orbital angular momentum during the merger is significantly larger than the intrinsic one.

The maps of line-of-sight velocity dispersion in the right column of Fig. 6 show considerable variation among the different simulations without any clear trend: some remnants have a maximum dispersion in the center while others have the maxima at larger distances. It seems that the complicated structure of the dispersion maps may be used as an indicator of the merger origin of the galaxy even after many Gyr of evolution.

4.2. Triaxiality

In order to study the evolution of the shape of the merger remnants, we again analyzed each dwarf separately selecting the stars inside the sphere of 2 kpc cen-
Fig. 7.— Evolution of the axis ratios and the triaxiality parameter for Dwarf 1 in different simulations. The gray horizontal lines in the lower two panels separate the regions of oblate, triaxial and prolate shape. The blue dashed curve corresponds to Dwarf 2 of simulation I90VY2.

Fig. 8.— Position angles of the intermediate axes of the stellar components for the four simulations which exhibit figure rotation. The angle is measured in the $YZ$ plane during the last 5 Gyr of each simulation.

The most dramatic change of the shape of the dwarfs happens around the second passage (approximately at $\sim 4$ Gyr). The ratio $b/a$, which is equal to unity at the beginning, slightly drops to values between about 0.8 and 0.9 for all simulations. The evolution of $c/a$ is more interesting. It grows from the original value of 0.12 up to the value ranging from 0.43 for I90VY2 (Dwarf 1) to 0.86 for I60R. For radial mergers, there is a simple rule for the behavior of $c/a$: the final ratio decreases when the initial angle between the angular momenta of the dwarfs increases, i.e., the merger remnants become thinner. For merger I90VY2 $b/a$ remains similar for both dwarfs but $c/a$ is significantly different (0.43 for Dwarf 1 and 0.73 for Dwarf 2). In the later stages of the simulations, all dwarfs can be classified as triaxial. Only I90VY1 crosses the line of the oblate shape in several time steps and Dwarf 2 of I90VY2 has more prolate values of triaxiality.

Referring again to Fig. 7 we note that the shapes of the merger remnants also differ in terms of their boxiness. In this respect, the dependence seems to be the strongest for the radial mergers. Clearly, the simulation with the dwarf disks oriented most vertically (I60R) with respect to the merger axis the isodensity contours are most boxy. In order to make this statement more quantitative we calculated the Fourier mode $A_4$ of the surface distributions of the stars (such as those shown in the left column of Fig. 6) for all simulations. The amplitude of the $m$th Fourier mode is given as

$$A_m = \frac{1}{N} \left| \sum_{j=1}^{N} \exp(im\phi_j) \right|$$

where $\phi_j$ are the particle phases in the projection plane and $N$ is the total number of particles. It turns out that over the last few Gyr of evolution $A_4 \approx 0.06$ for I60R while it is at least a factor of two lower for the other simulations. This shape must originate from the orbital structure of the merger remnant and we discuss this issue further in the following sections.

5. ORBITAL STRUCTURE

5.1. Figure rotation
Although the ratios of principal axes do not vary significantly over the last 5 Gyr for all simulations, all but I90VY2 show clear figure rotation around the major $x$ axis. The orientation of the major axis remains stable for the whole period of 5 Gyr and it coincides with the collision ($X$) axis for radial mergers and is inclined by 22 deg from the collision axis for I90VY1 but remains in the $XY$ plane. The evolution of the position angles of the intermediate axes for these four simulations are plotted in Fig. 8. For the purpose of these measurements we computed the principal axes for the combined stellar components from both dwarfs in each simulation.

The periods of rotation of the intermediate (and short) axes are 1.7, 2.2, 6.0, and 3.7 Gyr for I60R, I90R, I120R, and I90VY1, respectively. The speed of the figure rotation is correlated with the rotation of stellar particles around the long axis (see Fig. 4) but the particles rotate at a higher speed (at least for the inner 2 kpc). Also the direction of the particle rotation is the same as the figure rotation.

The origin of the figure rotation can be traced to the tidal distortion of the disk just before the first encounter. We illustrate this in Fig. 9 which displays stellar density in simulation I90R in three projections along the $Z$, $Y$ and $X$ axis of the simulation box. The upper row shows the projections just before the first passage at 1.95 Gyr and the bottom row illustrates the situation soon after the two disks merged, at 5.3 Gyr. The upper left panel of the Figure (view along the $Z$ axis) shows the distortion of the disks due to the tidal force acting before the merger. Since the stellar particles in both disks are moving upwards in this plot in the parts of the disks that are already in touch, the tidal force distorted the disk so that the upper parts are closer than the lower ones. This results in the tumbling (clockwise around the $X$ axis) of the elongated shape after the merger seen in the lower right panel (view along the $X$ axis).

Simulation I90VY2 has the major axis inclined by 67 deg with respect to the $X$ axis and lies in the $XY$ plane also being stable for the last 5 Gyr of evolution. The position angles of the other axes vary by only about 30 deg over the last 3 Gyr so this merger remnant does not show any significant figure rotation.

5.2. Orbit classification

In this subsection, we focus on simulations which exhibit significant prolate rotation, so we exclude I90VY2 from further analysis.

At the beginning of the simulations stellar particles are situated in inclined disks on nearly circular orbits. During the merger particle orbits are transformed to form an object with a shape that can be well approximated by a triaxial ellipsoid. In static triaxial potentials most particle orbits belong to one of a few major families: box orbits, short-axis tube orbits, and inner and outer long-axis tube orbits (de Zeeuw 1985). Schwarzschild (1982) also constructed a model of the triaxial ellipsoid with figure rotation around the short axis by properly populating different orbit families. Classifying orbits in a non-static potential is more difficult.

We performed a simplified classification of particle orbits using the last 4 Gyr of the simulations when the galaxies are already merged. We defined one orientation of the coordinate system $(x, y', z')$ which coincides with the actual principal axes of the galaxy only at one or few particular moments. For the rest of the time only the major axis is along the $x$ coordinate.

We adopted modified criteria of orbit classification from Schwarzschild (1993) as recently used by Gajda et al. (2013). Particles that keep a constant sign of the $x$-component of the angular momentum, $L_x$, are marked as long-axis tubes. Since the direction of the short axis is not stable, short-axis tubes are not classified in our case.

We also find orbits with low average values of the $x$, $y'$, and $z'$-component of the angular momentum. Specifically, we require the sum of these average values, $L_{xy/z'}$, to be less than 0.1 $M_\odot$ kpc$^2$ Myr$^{-1}$ (for comparison, in all outputs almost all particles inside 2 kpc have current total angular momentum smaller than 1 $M_\odot$ kpc$^2$ Myr$^{-1}$). When the figure rotation is present the box orbits acquire some net angular momentum (Schwarzschild 1982) thus we call this group just low angular momenta orbits. It
is worth noting that $L_y$ and $L_z$ of most of the particles average out to zero and $L_{xy'/z'}$ is typically dominated by the average value of $L_x$.

The rest of the particles, which do not fall into one of the above categories, are marked as other. These particles have $L_{xy'/z'} > 0.1 M_\odot \text{kpc}^2 \text{Myr}^{-1}$ and at the same time they do not keep a constant sign of $L_x$ for the duration of the last 4 Gyr of the simulation.

Fig. 10 shows fractions of the three types of orbits as a function of radius in the final outputs of the simulations. The fraction of long-axis tubes correlates tightly with the amount of the mean rotation velocity of particles discussed in section 4.1. Galaxies with higher rotation have faster increase of the fraction of long-axis tubes with radius, mainly at the expense of the low angular momenta orbit family.

5.3. Orbital frequencies

For the long-axis tubes we computed the average angular and radial frequency of the stellar motion in the plane perpendicular to the major axis. The calculations were done for the period of the last 4 Gyr of each simulation. The angular frequency, $\omega$, was computed in each time step as $v_r/r_{yz}$, where $v_r$ is the tangential part of $(v_y^2 + v_z^2)^{1/2}$ and $r_{yz} = (y^2 + z^2)^{1/2}$. We defined the radial frequency, $\kappa$, as $1/T_{\text{avr}}$, where $T_{\text{avr}}$ is the average time period between two subsequent maxima of $r_{yz}$.

The distributions of the stars in the $\omega\kappa$ plane for all four simulations are shown in the left panels of Fig. 11. Only stellar particles with orbits classified as long-axis tubes are included. The right panels show the distribution of the ratio $\kappa/\omega$ for the same particles. Two branches are clearly visible in the plots. For all simulations the branches have a similar slope of $\kappa(\omega)$: around 1.8 for the upper branch and 1.4 for the lower one. Two sub-families are known to exist among the family of long-axis tube orbits in triaxial systems: the inner and outer long-axis tubes. A natural expectation therefore is that the two branches correspond to these two sub-families.

In order to check this interpretation we tried to identify the inner and outer long-axis tubes using the criteria from Gajda et al. (2015). For an orbit to be classified as an inner tube, the absolute value of the $x$-coordinate of the particle when it reaches the maximum value of $r_{yz}$ must be larger than the corresponding value when $r_{yz}$ has a minimum, that is, $|x(r_{yz,\text{max}})| > |x(r_{yz,\text{min}})|$. For the outer tubes, the inverse condition is fulfilled: $|x(r_{yz,\text{max}})| < |x(r_{yz,\text{min}})|$.

We find that indeed the outer tubes are more likely to be found in the upper branch of the $\kappa(\omega)$ plot while the inner tubes are typically situated in the lower one. By visual inspection of some orbits we see that this rule does not identify the tubes correctly in all cases as particle orbits are not always regular: they are still being disturbed by perturbations related to the past merger or by the time-dependent potential due to figure rotation. Fig. 12 shows two examples of orbits from the upper branch of $\kappa(\omega)$ in the top row and from the lower branch in the bottom row that were classified as the outer and inner long-axis tubes respectively. Clearly, the shape of the orbits is as expected for these two sub-families, i.e. the outer tubes are convex while the inner ones are concave.

Comparing the distributions of the ratio $\kappa/\omega$ in the
As already discussed by Lokas et al. (2014), although using only an exactly prograde orientation of the disk, the main and most important difference between the two scenarios seems to be the occurrence of prolate rotation which is present in dwarfs formed by mergers and absent in the tidal stirring simulations. We are not aware of any mechanism which could induce prolate rotation only via tidal interaction of a disky dwarf with a host galaxy. To support this statement, in Fig. 13 we plot the evolution of the mean rotation velocity around the major axis, $v_x$, of the stellar component of the dwarfs in the tidal stirring simulations. The measurements invariably yield very low values of this quantity, of the order of 1 km s$^{-1}$ at most, not only for the prograde case but for the other inclinations as well. As expected, the signal is strongest for the perpendicular orientations of the disk, i.e. in simulations TS-I90 and TS-I270. We also note that the amount of prolate rotation is not related in any way to whether and how fast a bar forms and evolves in these simulations. For comparison, we also include in this Figure the same quantity measured for Dwarf 1 of our merger simulation I90R from Fig. 4 where the evolution of $v_x$ for all the merger simulations is shown. In the tidal stirring simulations, the rotation around the minor axis, $v_z$, is always the dominant component of the rotation even though it is gradually diminished and replaced by random motions as a result of the evolution (see the top panel of Figure 2 in Lokas et al. 2015).

Fig. 13 shows the surface brightness and kinematics maps for tidally stirred dwarfs from simulations TS-I0 and TS-I270 after 6.5 Gyr of evolution (i.e. at the fourth apocenter) viewed along the intermediate and minor axis ($y$ and $z$, respectively). The maps are analogous to those shown in Fig. 4 for the merger remnants, we kept the same range of the color scale as well as distances between the isocontours for the corresponding quantities. Only the displayed area is smaller here because the tidally stirred dwarfs are diminished in size at this late stage of evolution due to tidal stripping. The maps of the mean velocity (middle columns) clearly show that the rotation, if present, is seen always along the major axis of the projected galaxy so the stars rotate around the minor axis. The velocity dispersion of the tidally stirred dwarfs (right columns of Fig. 13) is generally lower and more regular than in our merger remnants where the dispersion maintains a more complicated structure even many Gyr after the merger. In order to detect these irregularities one would need a good spatial resolution for the kinematics and we comment on this issue further in the next section.

The surface density maps for the tidally stirred dwarfs in the left columns of Fig. 14 show the remnant bar in the center. In comparison with these, the merger remnants have overall more regular shapes with more boxy isocontours. However, the boxiness is suppressed for non-
radial mergers and larger initial angles between angular momenta of the progenitor discs. In addition, the bar induced during the tidal stirring can make the isophotes look boxy as well if only the brightest central part of the galaxy was available for observation, so this feature probably cannot be used as an indicator of the merger origin. In the case of low surface brightness galaxies, such as And II, the boxy shape would be particularly challenging to detect.

In principle, one more feature that could discriminate between the tidally stirred and merged objects, as advertised by Tomozeiu et al. (2015), is the density profile in the outskirts. It has been shown (e.g. Lokas et al. 2013, 2015) that tidally stirred galaxies develop a flattening of the density profile due to the transition between the stars which are bound to the dwarf and the tidal tails. However, the presence and detectability of this transition depends on the number of issues. First, the transition in the form of the break radius in the stellar density profile is not seen in dwarfs in non-prograde orbital configurations (see Figure 6 in Lokas et al. 2013). Second, the tails will not be visible if they are aligned with the line of sight of the observer and this unfortunately is the case for most of the time for dwarfs on different orbits (Klimentowski et al. 2009 Lokas et al. 2013). Third, the tidal tails are usually very faint and have been convincingly detected only for the Sgr dwarf. Moreover, tails produced by the merger can, at some stages, mimic this transition. Furthermore, one cannot rule out the case of the merger remnants being subsequently tidally stirred by the host galaxy.

7. TOWARDS A COMPLETE MODEL OF AND II EVOLUTION

In this section we compare the results of our merger simulations to the real data for And II and discuss the possible scenario for its formation. In order to reproduce the observational data, we require the simulated merger remnant to show: (1) the rotation along the minor axis at the level of 10 km s$^{-1}$ at the maximum, which should be comparable to the maximum value of the line-of-sight velocity dispersion, (2) no significant rotation along the major axis, (3) the same kinematics for stars originating from both progenitors, (4) the shape of rather low ellipticity. The observational data cover the area of about 2 kpc in radius.

The measured kinematics of And II (Ho et al. 2012) shows significant variability, while the equivalent values taken from the final outputs of the simulations are rather smooth if they are derived using all stellar particles along the major/minor projected axis about 4 kpc long. In this case even the fluctuations of the dispersion are averaged out for the final outputs. Therefore, in order to reproduce the observed kinematics we explored the kinematics from all simulation outputs (after the merger) as well as different lines of sight along which these outputs are ‘observed’. Best matches of the observed kinematics (in terms of the lowest $\chi^2$) for all simulations are shown in Fig. 15. In this comparison we again exclude the non-radial simulation I90VY2 which failed to produce significant amount of prolate rotation. The sizes of the bins for the simulated data correspond to those used in observations. The best matches come from times 4.6–7.1 Gyr since the beginning of the simulations. In all cases we also verified that for the chosen line of sight the ellipticity of the galaxy is in the range of about 0.1–0.2, as required by the data (McConnachie & Irwin 2006; Ho et al. 2012; Salomon et al. 2015).

In general, earlier stages of the merger can reproduce the fluctuations in the measured kinematics better. Shortly after the merger, the galaxy is unrelaxed with many shells and streams visible that formed as a result of the collision. An example of the merger remnant image corresponding to the output at 4.7 Gyr with the best-fitting kinematics for simulation I90R is shown in the left panel of Fig. 17.

However, we are able to reproduce the fluctuations in the kinematics even for the final outputs corresponding to times a few Gyr after the merger if we recall that the real data are based on a much lower number of stars. For this comparison, we pick a subsample of about 500 stellar particles which match the number of stars used to derive the kinematics of And II in Ho et al. (2012). Again we use the same binning and select the stellar particles so that their distribution roughly covers the area used in the observations. In all other aspects, the choice of the particles is random. We repeat the subsample selection...
several hundred times for different lines of sight and find
the ones that match the data best.

Examples of good matches of the simulated data to
the observed kinematics are shown in Fig. 16 for cases
with ellipticity around 0.1–0.2. This proves that the ob-
served fluctuations could be still consistent with the re-
laxed stage of the merger remnant. An image of such
a relaxed merger remnant in a late stage is shown in
the right panel of Fig. 17 for simulation I90R at 10 Gyr
where it can be directly compared to the analogous image
at 4.7 Gyr in the left panel. These outputs and lines of

sight correspond to the kinematics shown with red lines
in Fig. 15 (for 4.7 Gyr) and Fig. 16 (for 10 Gyr).

Besides the measured shape and kinematics, addi-
tional constraints on the possible scenario for the for-
mation of And II come from its recently measured star
formation history (Vargas et al. 2014; Weisz et al. 2014;
Gallart et al. 2015). The measurements point to the ex-
istence of the intermediate-age stellar population dated
5–8 Gyr ago. Although we do not model star formation
processes here, given the comparisons discussed above
and these additional constraints we may speculate on
the possible general scenario for the formation of And II.
And II most likely formed as a result of a merger be-
tween two disky gas-rich dwarf galaxies of similar mass
and disk properties. The disks must be inclined by 90±30
deg in order to possess significant components of angu-
lar momentum along the merger axis. The two galaxies approached each other on a nearly radial orbit with a rather low relative velocity forming a bound pair. The existence of such pairs of subhalos has been confirmed in recent studies of simulations reproducing environments similar to the Local Group (Klimentowski et al. 2010; Kazantzidis et al. 2011; Deason et al. 2014; Wetzel et al. 2015). Since the occurrence of such groups is more likely outside the virial radius of big galaxies, the merger probably occurred before the galaxies were accreted by M31, a few Gyr ago. The merger induced the secondary burst of star formation, mainly in the center of the merger remnant, converting some of the gas into stars in a similar fashion as in the well-studied mergers between normal-size galaxies (e.g. Cox et al. 2006; Hoffman et al. 2010). The new stars gave rise to the distinct stellar population with a more concentrated density profile that can be identified with the intermediate-age stellar population seen in the data. These younger stars should contribute about 30% of the stellar mass in the central region (Gallart et al. 2013).

Further evolution of the merger remnant remains an open question. However, since we do not see any young stars in And II and no gas is detected in it at present, we may suppose that the star formation ceased a few Gyr ago, either quenched by internal processes such as supernova feedback or by environmental effects such as ram pressure stripping, if the merger remnant was accreted by M31. The present distance of And II from M31 is about 180 kpc and their relative line-of-sight velocity is of the order of 100 km s$^{-1}$ i.e. low enough for And II to be a satellite of M31, but no strong constraints are available on its orbit. However, Shaya & Tully (2013) find a solution for the Local Group galaxy orbits (see their Figure 13) where And II has experienced a close passage near M31 which may have stripped its gas. Nevertheless, this interaction could not be too strong so that And II could preserve its prolate rotation and probably did not lead to any new starburst. Cases of accretion of merger remnants by bigger hosts have been also confirmed in the simulations of the Local Group and Milky Way environments (Kazantzidis et al. 2011; Tomozeiu et al. 2015).

The scenario we sketched here can be developed into a full model of a gas-rich merger only by incorporating gas dynamics and star formation. The outcome of such simulations will depend on a number of parameters like the threshold for star formation and the amount of feedback. These parameters can in principle be adjusted to reproduce the observed mass fraction of the newer stellar population. We expect that such a model will be able to preserve the prolate rotation of the old stellar population but it remains to be seen what will be the kinematics of the younger stars. A more complete scenario for the formation of And II will be described in detail by S. Fouquet et al. (in preparation).

8. SUMMARY AND CONCLUSIONS

In this work we studied the origin of prolate rotation in dSph galaxies forming via mergers of two disky dwarfs. Our work was motivated by the discovery of such type of rotation in the dSph galaxy And II. Lokas et al. (2014a) demonstrated that this kind of rotation can indeed result from a merger between two disky dwarf galaxies. They proposed a detailed, but rather fine-tuned scenario with very special initial conditions. Here we showed that these initial conditions can be varied to some extent and can still reproduce the main observational properties of And II.

Masses of the luminous parts of the dwarfs were chosen so that their combined luminosity is similar to
what is measured for And II. The dark matter components were adjusted so that the kinematics of the remnants matches the observations. In addition, [Lokas et al. (2014a)] showed that the different density profiles of the two stellar populations could be reproduced by adopting different initial scale-lengths of the disks of the dwarfs. We did not address this issue in the present paper and for simplicity assumed that the two progenitors are identical in terms of structural parameters and masses.

The evolution of the three radial mergers we considered is straightforward to interpret. In these simulations the initial conditions are symmetrical for both dwarfs. The initial angle between the angular momenta of the dwarf disks determines how much of the disk rotation is transformed into the prolate rotation of the merger product. With the lower value of the angle, corresponding to the more vertical orientation of the disks, we get more prolate rotation as well as a more boxy shape of the surface density of the galaxy. The dispersion and, more importantly, the rotation in simulation I120R is not high enough to match the data while I90R and I60R both reproduce the line-of-sight kinematics of And II satisfactorily.

From non-radial simulations (I90VY1 and I90VY2) we see that the perpendicular component of the relative velocity, corresponding to the orbital angular momentum, cannot be increased too much. Both simulations have the radial component of the relative velocity of 8 km s$^{-1}$. In simulation I90VY1, with the perpendicular velocity component of 1 km s$^{-1}$, the merger remnant still roughly meets the observation constraints (although with less rotation and smaller dispersion than observed). The remnant of simulation I90VY2, with the perpendicular velocity component of 2 km s$^{-1}$, does not reproduce the data well: it has very small rotation and the kinematics of stars originating from different dwarfs is significantly different. We note that for non-radial mergers the initial conditions were set up so that the merger is prograde for one progenitor and retrograde for the other one. In combination with a larger orbital angular momentum, this resulted in a very different evolution in simulation I90VY2 compared to I90VY1.

All remnants showing significant prolate rotation have similar orbital structure, dominated by box orbits in the center of the galaxy and by the long-axis tubes in the outer parts. However, there are subtle differences depending on the initial conditions: the transition from the box orbits to the long-axis tubes takes place at smaller radii for remnants with stronger prolate rotation. In addition, the remnant with the highest rotation and the most boxy shape (I60R) turns out to possess a noticeably bigger contribution of inner versus outer long-axis tubes than any other remnant.

We conclude that prolate rotation may be produced in mergers with a variety of initial conditions. The inclination of the disks with respect to the orbit must be significant in order to provide enough angular momentum in the remnants but can be varied by a few tens of degrees, producing remnants of slightly different kinematics and shape. Some orbital angular momentum during the merger, up to a factor of a few of the intrinsic angular momentum of the merging disks, is also allowed and does not destroy the symmetry between the two components of the remnant.

We compared the predicted properties of our merger remnants to those characteristic of galaxies evolving in the vicinity of bigger host and affected by tidal stirring. Although a number of features, such as the boxiness of the shape, irregularities in the kinematics and strong tidal extensions, could possibly help us to distinguish the dSph galaxies formed in the two scenarios, they are generally not accessible with present observational techniques. We propose that the only reliable feature that can act as a fingerprint of the past merger is the presence of prolate rotation such as the one observed in And II. Such type of rotation can not be induced via tidal stirring at a significant level even for a variety of orbital configurations.

We have also compared our merger remnants to the real data available for And II. We find that in order to reproduce the data the merger could not have happened recently, but rather a few Gyr ago. This statement is supported by the fact that the surface brightness distribution in And II is rather regular without obvious distortions and the need to be consistent with the recently measured star formation history of the galaxy which points to the presence of an intermediate-age, rather than a young, stellar population. The subsequent evolution of And II should have been rather quiescent in order to preserve prolate rotation, although it may have interacted with M31, which led to the stripping of its gas.

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REFERENCES
Amorisco, N. C., Evans, N. W., & van de Ven, G. 2014, Nature, 507, 335