AN INCREASE IN THE MASS OF PLANETARY SYSTEMS AROUND LOWER-MASS STARS

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\textit{Manuscript in prep. for ApJ}

1. INTRODUCTION

The \textit{Kepler} spacecraft has unearthed a population of planets at short orbital periods that orbit the majority of stars in our galaxy (e.g. Borucki et al. 2011; Howard et al. 2012; Fressin et al. 2013; Burke et al. 2015). This population is significantly distinct in planet size, orbital period, and bulk composition from previously known planetary systems, including our solar system. The formation history of these “Super-Earths” or “mini-Neptunes” is still open to debate. They may have formed in situ in an up-scaled version of our solar system (Chiang & Laughlin 2013; Hansen & Murray 2013); they may have formed at larger distances from the star and migrated inward (e.g. Swift et al. 2013); or they formed through a combination of both processes (e.g. Hansen & Murray 2012; Alibert et al. 2013; Cossou et al. 2014).

Variations in the planet population with host star properties provide an avenue of discriminating between planet formation theories. Radial velocity surveys indicate that the occurrence of giant planets correlates strongly with host star mass (Johnson et al. 2010) and metallicity (e.g. Santos et al. 2000). These results are consistent with the core-accretion paradigm of planet formation, in which larger solid mass in higher-mass and higher-metallicity disks is necessary to form cores massive enough to start run-away gas accretion (e.g. Ida & Lin 2004; 2005; Dawson et al. 2015).

The presence of a large population of planets smaller than Neptune (“failed cores”) at shorter orbital periods does not match the predictions of the core-accretion model (Howard et al. 2010, 2012). Their presence does not correlate with stellar metallicity (Sousa et al. 2008; Buchhave et al. 2012; Schlaufman 2015; Buchhave & Latham 2015), though weaker trends with metallicity are evident (Dawson et al. 2015; Adibekyan et al. 2015). Surprisingly, the occurrence rate of these sub-Neptune sized planets increases for lower-mass stars (Howard et al. 2012; Mulders et al. 2015), opposite to the trend for giant planets. Qualitatively, this does match the prediction of in-situ formation models, where more numerous, but smaller planets form in low-mass disks around low-mass stars (e.g. Wetherill 1996; Kokubo & Ida 2002; Raymond et al. 2007; Ciesla et al. 2015). In agreement with these predictions, a lack of planets larger than \( \sim 2.5 R_{\oplus} \) has indeed been noted around the lowest-mass stars in the \textit{Kepler} sample (Dressing & Charbonneau 2013, 2015; Morton & Swift 2014).

In this paper, we place these results into context by investigating how the planet radius distribution varies as a function of spectral type, and hence stellar mass. We explore and reject the hypothesis that higher occurrence rates toward lower mass stars are due to a redistribution of mass into more numerous, smaller planets. We make a quantitative comparison between the close-in planet population and different planet formation models.
Table 1

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<th>$R_p$ [cm]</th>
<th>$P$ [day]</th>
<th>$f_{occ}$</th>
<th>$T_{\text{eff}}$ [K]</th>
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Table 1 is published in its entirety in the electronic edition of the Astrophysical Journal. A portion is shown here for guidance regarding its form and content.

Planet occurrence rates are calculated using the methodology described in Mulders et al. (2015). We use the planet candidate sample from Mullally et al. (2015), which is currently the preferred catalogue for occurrence rates studies (e.g. Burke et al. 2015). In short, for every main-sequence star observed by the Kepler spacecraft, we calculate whether a planet of given radius, $R_p$, and orbital period, $P$, could be detected based on the combined signal to noise of all transits during the time the star was observed. The stellar parameters ($T_{\text{eff}}, R_*, M_*$) are taken from Huber et al. (2014). The stellar noise during the duration of a single transit is interpolated from the Combined Differential Photometric Precision (Christiansen et al. 2012) at 3, 6, and 12 hour time scales, downloaded from the MAST archive on December 12th 2013. The occurrence rate $f_{occ}$ in the range $\{R_p, P, T_{\text{eff}}\}$ is the ratio of the number of KOIs over the number of stars were planets are detectable, multiplied by the geometric transit probability. We treat all KOIs as real planets, consistent with the low false positive rate in the Kepler data (Fressin et al. 2013). In the following paragraph, we describe in detail where we deviate from the assumptions in Mulders et al. (2015).

We use the KOI list spanning quarters Q1-Q16 (4 years) from Mullally et al. (2015), replacing the Q1-Q8 list (2 years) from Burke et al. (2014) in our previous work. Aside from doubling the observing time baseline, this new version of the pipeline has an improved detection efficiency at low transit signal-to-noise (S/N), with $f_{occ}$, $R_p$, $P$, $T_{\text{eff}}$ are provided in Table 1.

Figure 1. Planet radius distribution for orbital periods between 2 and 50 days for all main-sequence stars in the Kepler sample. $\pm \sigma$ error bars are calculated from the square root of the number of KOIs in each bin. The sample of stars becomes incomplete below ~ 1 $R_\oplus$. The red dotted line shows the best-fit power-law in planet radius ($k_R = 2.9, \alpha = -1.9$) derived by Howard et al. (2012). The green dashed line shows the best-fit power-law between 2.4 - 8 $R_\oplus$ with $k_R = 30, \alpha = -3.3$. The occurrence rates from Mulders et al. (2015), based on the first eight quarters and shifted by 0.06 dex in planet radius for clarity, are shown for reference. These rates show good agreement for planets larger than 2 $R_\oplus$, while our previous work underestimated the amount of smaller planets.

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of 3865 K, 5310 K, 5980 K, and 7320 K as upper bounds for M, K, G, and F stars, respectively. Occurrence rates for each KOI in both the full sample and spectral type subsamples are provided in Table 1.

2.1. Planet radius distribution

We calculate the planet radius distribution between orbital periods of 2 to 50 days. The inner edge of 2 days is chosen because there is a clear lack of large ($> 2 R_\oplus$) planets at shorter orbits, which might be a signature of photo-evaporation (e.g. Sanchis-Ojeda et al. 2014). To include planets down to one Earth radius even around M stars, we choose an outer period cut of 50 days. We use orbital period, rather than semi-major axis, to define this region because Mullally et al. (2015) have shown that the characteristic feature in the occurrence rates with distance from the star scales with orbital period when considering different stellar-mass sub-
samples. This range encompasses the peak in detected KOIs, which lies roughly at 10 days, optimizing the detection statistics.

We construct the planet radius distribution by summing the occurrence rates in an orbital period and planet radius bin. The default orbital period bin is 2-50 days as described above, and planet radius bins are equally spaced in log space with 4 bins per factor 2 increment. Errors are given as the square root of number of KOIs in each bin. The sample of stars becomes incomplete below \( \sim 1 R_{\oplus} \).

Figure 2. Planet radius distribution for orbital periods up to 50 days for the cool star sample, compared to [Mulders et al. (2015)](yellow symbols, offset by 0.06 \( R_{\oplus} \) for clarity) and [Dressing & Charbonneau (2015)](the height of the blue box represents the 1-\( \sigma \) error). The improved estimate of the detection efficiency in [Dressing & Charbonneau (2015)] yields higher planet occurrence rates for the coolest stars. 1-\( \sigma \) error bars are calculated from the square root of the number of KOIs in each bin. Figure 1 shows the planet radius distribution for the entire Kepler sample of main-sequence stars. These rates show overall good agreement with those in [Howard et al. (2012)](who fit a power-law in planet radius for planets within \( P < 50 \) days between radii \( 2-22.6 R_{\oplus} \) with an index \( \alpha = -1.9 \)). Our finer binning, larger number of KOIs, and completeness down to smaller planets reveals additional structure in this distribution: a plateau below \( 2 R_{\oplus} \), a steep dropoff towards large planet radii, and a flattening between \( 8-16 R_{\oplus} \). We identify a steeper slope of \( \alpha = -3.2 \) in a narrower range of radii, \( 2.4-8 R_{\oplus} \), compared to [Howard et al. (2012)](2012).

The occurrence rates are consistent with our previous work (Mulders et al. 2015) for planets larger than \( 2 R_{\oplus} \), but significantly higher for smaller planets. The addition of many smaller planet candidates in the Q1-Q16 catalogue boosts occurrence rates in this regime, and our previous estimate of the detection efficiency (a linear ramp between SNR of 6 to 12) was not sufficient to correct for this. We also compare occurrence rates for the cool star sub-sample (\( T_\text{eff} < 4000 \) K) to those of [Dressing & Charbonneau (2015)] and [Mulders et al. (2015)] in Figure 2. The rates are consistent with our previous work within errors. The rates from [Dressing & Charbonneau (2015)] are systematically higher, most likely due to their better estimate of the detection efficiency in their own pipeline, which does not reach 100%, boosting occurrence rates for planets at all signal-to-noise ratios. Christiansen et al. (2015) found that the detection efficiency is different for non-FGK stars, but the detection efficiency for M stars could not be accurately determined. This lower detection efficiency may indicate that the occurrence rates for M stars are currently underpredicted.

2.2. Conversion to planet heavy-element mass

To test if the higher occurrence rate of planets around low-mass stars is due to a re-distribution of the same mass into more numerous, smaller planets, we have to convert observed planet radii into planet (heavy-element) masses (e.g. Najita & Kenyon 2014). Though a one-to-one conversion is not possible due to intrinsic scatter in mass-radius based on planet composition (e.g. Lopez & Fortney 2014), we will use the average mass-radius to represent our statistical ensemble. Planets smaller than \( \sim 1.5 R_{\oplus} \) have compositions that are consistent with rocky (Rogers 2015; Dressing et al. 2015). Larger planets contain significant gaseous atmospheres and have a mass-radius relation that is roughly linear (e.g. Wu & Lithwick 2013), compared to a quadratic relationship based on a fit to solar system planets (Lissauer et al. 2011). Planets up to \( 3 R_{\oplus} \) are significantly less dense than Neptune, with their masses set by their rocky core and their radii set by a \( \sim 1\% \) gaseous envelope (e.g. Wolfgang & Lopez 2014). For larger planets, gaseous atmospheres contain a non-negligible fraction of the planet mass. Estimates of the heavy-element mass of planets between Neptune and Jupiter sizes range from \( 10-100 M_{\oplus} \) (Miller & Fortney 2011).

We use the empirical mass-radius relation from (Weiss & Marcy 2014, hereafter WM14), derived for planet radii smaller than \( 4 R_{\oplus} \), to represent the heavy-element mass of Kepler planets. Figure 3 shows that this mass-radius relation happens to correctly estimate the planet heavy-
element mass for larger planets as well: for radii of 10 $R_\oplus$, it gives a mass of $\sim 23 M_\oplus$, surprisingly close to the median heavy-element mass of $\sim 22 M_\oplus$ in Miller & Fortney (2011). We also compute planet masses using the best-fit single-power-law relation from (Wolfgang et al. 2015, hereafter WRF15). This relation predicts overall higher masses and has a steeper slope. It predicts a mass for giant planet much larger than the heavy-element mass, so we use a maximum mass of 22 $M_\oplus$ to represent the heavy-element component, consistent with the median heavy-element mass for giant planets in Miller & Fortney (2011). Because there is no separate treatment for rocky planets, the masses of planets below 1.5 $R_\oplus$ are overestimated with respect to WM14.

Figure 4 shows the cumulative distribution function or CDF of planet radii, compared with an estimate of the planet heavy-element mass as described above. The most apparent feature in the planet radius CDF is the turnover at $\sim 3R_\oplus$, and it is clear the 90%-95% of the planets are smaller than 3–4 $R_\oplus$. Rocky planets ($<1.5 R_\oplus$) constitute at least half the planet population. For comparison, the mass distribution according to quadratic mass-radius relation from (Lissauer et al. 2011) is shown to highlight that the total mass in planets remains dominated by the gaseous envelopes of giants. 60-70% of the total mass is concentrated in planets larger than 3–4 $R_\oplus$.

The distribution of heavy-elements between planets of different sizes varies. Giant planets have more heavy elements — though as a smaller fraction of their total mass — and the largest planets contain 20%-30% of the total heavy-element mass. The bulk of the heavy-element mass ($\sim 70\%$) is concentrated in the cores of mini-Neptunes ($1.5R_\oplus$–$2.8R_\oplus$), independent of the adopted mass-radius relation. About 10% is found in super-earths ($1–1.5R_\oplus$). The largest discrepancy between the WM14 and WRF15 relation occurs at these smallest radii, where the latter predicts double the amount of mass in planets $<1.5R_\oplus$. This difference arises mainly because we have not included the physical mass constraint for rocky planets in the WRF15 relation. Even though the incomplete sample of sub-earth-sized planets represents 30% of the number of planets, their masses are too small to contribute. According to the model of Zeng & Sasselov (2013), the mass difference between a 0.7$R_\oplus$ and 1.2$R_\oplus$ planet is a factor 20. Unless the planet occurrence shows an order of magnitude increase below 1 earth radius, there is no significant contribution from small planets to the total mass. This means that Kepler has detected the bulk of the planet heavy-element mass out to a 50-day orbital period, and 80% of this mass is located in planets with radii between 1 – 3$R_\oplus$.

3. SPECTRAL-TYPE DEPENDENCIES

3.1. Higher planet occurrence rates around M stars

The top panel of figure 5 shows the planet radius distribution of M dwarf stars compared to main-sequence FGK stars. Upper limits are calculated as the occurrence
of a planet with a radius and orbital period corresponding to the logarithmic center of each grid cell. Because the binned version does not capture all the structure in the data, we also show the regression curve based on variable-bandwidth kernel density estimation in the bottom panel. This approach of representing the data is similar to that of Morton & Swift (2014), but we use a kernel density estimator based on a maximum width of 0.1 dex and the distance to the 5th nearest neighbour. The 1 − σ confidence interval is calculated by adding the contribution of each kernel in quadrature and taking the square root of the total. Both distributions show a plateau in occurrence rate between 1 − 2.8 $R_{\oplus}$ and a dropoff towards larger planets. The occurrence of planets in the plateau is a factor of $\sim 3.5$ higher for M stars. The occurrence rate of larger planets (2.8 − 16 $R_{\oplus}$) is a factor two lower around M stars, best visible in the regression curve, roughly consistent with the linear scaling of giant planet occurrence with stellar mass from RV surveys (Johnson et al. 2010).

We note that the low number of detected large planets around M stars is not due to a signal-to-noise bias, as Kepler is more complete for large planets than for small ones. Instead, the low number of detected KOIs is a product of the lower number of M stars surveyed combined and an intrinsic lower planet occurrence rate. In other words, if a population of planets similar to that around sunlike stars was present, it would have been detected. Instead, the ratio of small to large planets is a factor 8 higher for M stars than for FGK stars, consistent with the increase in occurrence with spectral type of planets between 1 − 4 $R_{\oplus}$ in Mulders et al. (2015). These differences between G stars and K and F stars are significant at the 4.5 and 5.5 sigma level, respectively. There is no

Figure 6. Same as figure 4 for M dwarf stars in the Kepler sample. 95% of the heavy-element mass is concentrated in planets smaller than 2.8 − 4$R_{\oplus}$. The contribution of rocky planets (< 1.5$R_{\oplus}$) to the heavy-element mass is about 20%.

Figure 7. Planet radius distribution (left) and cumulative planet mass per star (right) for orbital periods between 2 and 50 days for M, G, K and F stars. The bins in the upper panel are twice as wide as in figure 4. 95% of the heavy-element mass around M stars is located in planets smaller than 2.8 − 4$R_{\oplus}$, in contrast to the 70%-80% in the full sample. Rocky planets amount to $\sim 10\%$ of the heavy-element mass, again implying that the contribution of planets below the detection limit to the total mass is negligible.

3.2. Differences between FGK stars

Motivated by the finding of a higher planet occurrence rate around M stars, we investigate the spectral type dependence of the planet radius distribution between F, G, and K stars. Figure 7 left panel shows the spectral type dependence of the binned planet radius distribution. Since the differences between FGK stars are significantly smaller than the difference with respect to M stars, we bin the planet radius to a coarser resolution. The occurrence rate in the plateau below 2.8 $R_{\oplus}$ increases from 0.27 ± 0.01, to 0.35 ± 0.01, to 0.46 ± 0.02, to 1.12 ± 0.12 for F,G,K, and M stars, respectively, consistent with the increase in occurrence with spectral type of planets between 1 − 4 $R_{\oplus}$ in Mulders et al. (2015). These difference between G stars and K and F stars are significant at the 4.5 and 5.5 sigma level, respectively. There is no
3.3. More heavy-element mass around lower-mass stars

We calculate the average heavy-element mass in planetary systems for the largest possible region in planet radius-orbital period diagram where Kepler is complete for spectral types M to F (See appendix A). The heavy-element mass locked in planetary systems in this region are listed in table 3 and shown in Figure 8 for each spectral type sub-sample. This mass increases from 3.6$M_⊕$ in F stars to 7.3$M_⊕$ in M stars and scales roughly proportional to the inverse of the median stellar mass in each spectral type bin which is listed in the same table. The inclusion of the 50-150 day region increases the total planet mass with respect to that of Figure 7, but we have tested that it does not change the trend with spectral type. For comparison, the estimated dust mass in protoplanetary disks shows the opposite trend with stellar mass (Moehanty et al. 2013, Andrews et al. 2013). Although dust disk masses are measured from and dominated by a region further away from the star, the scaling law with stellar mass is often assumed to be relevant for formation of close-in planets (e.g. Raymond et al. 2007). The agreement between dust mass and planet heavy-element mass for M stars is likely coincidental: surveys are insensitive to objects larger than a few centimeters, and it is likely that a larger reservoir of planetary building blocks is present in these disks (e.g. Najita & Kenyon 2014).

This trend is robust against the various assumptions that go into deriving it. Our estimates for the M star planet occurrence rates are lower than those in Dressing & Charbonneau (2015), most likely due to our overestimation of the pipeline completeness for M stars versus FGK stars. However, a higher planet occurrence rate for M dwarfs would only strengthen the observed trend. Adopting a different mass-radius relation increases the total estimated heavy-element mass, but does not affect the observed trend with spectral type (See Fig. 8). The only factor that could significantly change this result is if the mass-radius relation is dependent on spectral type. There are currently no indications that this is the case (Weiss & Marcy 2014), though only few measurements of M star planet masses and radii are available. To be consistent with a linear disk-stellar mass scaling, planets around M stars of sizes $\sim 1-3 R_⊕$ need to be 5-10 times less dense than around sun-like stars. Though we do not deem this scenario to be very likely, it would have interesting implications for planet formation theories.

4. DISCUSSION

The increase in the average mass of planetary systems toward low mass stars found in the Kepler data goes against the widely adopted assumption that planet masses scale with total disk mass and hence should decrease with stellar mass. In this section we will compare these results to the predictions of planet formation in-situ (4.1) and through migration of fully formed planets (4.2). We also show that we can exclude binarity (4.3) and long-period giant planets (4.4) as alternate explanations for the increased occurrence rates, and propose a scenario to explain these results (4.5, 4.6).

4.1. Comparison with in-situ formation

Kokubo et al. (2006) explored how changes in the disk surface density affect terrestrial planet formation...
between 0.5 and 1.5AU around a solar-mass star using N-body simulations. They fit a relation between the disk surface density $\Sigma$ and the number of planets, $n$, and their masses, $M_P$, that can form in situ in such a disk. Assuming the surface density is proportional to disk mass, the number of planets scales as $n \propto \Sigma^{-0.15}$. If we assume surface density is the only factor determining the number and mass of planets, the stellar mass range of a factor 2 probed in the Kepler data predicts an increase in the occurrence of planets of 10%, significantly smaller than the factor 3.5 derived in this work for $1-2.8$ $R_\odot$ planets. The predicted planet mass scale slightly steeper than linear, $M_P \propto \Sigma^{1.1}$. Factoring in the planets mass-radius distribution, $R_P \propto M_P^{0.83}$, a systematic shift in the planet radius distribution of a factor of $\sim 2$ between M stars and FGK stars is predicted, yet such a trend is not present in the Kepler data (see Figure 5).

The scaling laws from Kokubo et al. (2006) do not take into account differences in stellar mass, which may lead to a different scaling relation between surface density and number of planets. We also compare our result with the N-body simulations of Ciesla et al. (2015), who simulate the formation of terrestrial planets around stars of various masses. They assume the total surface density of planetary building blocks scales with stellar mass. Although these simulations cover larger orbital periods and smaller planet radii than accessible to Kepler, they do provide insight in how the number of planets scales with stellar mass and surface density in the context of in-situ formation. Between 0.5 and 1.5 AU, the simulations for a sun-like star contain 14 planets. The corresponding orbital period range for the 0.4 $M_\odot$ star, representative of the M star sample, contains 18 planets. Again, the decrease in surface density does not increase the number of small planets formed in situ by a large enough number (1.3 versus 3.5) to explain the increased occurrence of planets around low-mass stars. In addition, these planets are 3-5 times less massive, a feature not seen in the planet radius distribution. Therefore, existing in-situ models do not appear to predict the general trend in planet occurrence rates and stellar mass found in our study.

### 4.2. Comparison with planet migration

Swift et al. (2013) proposed the convergent migration of fully-formed planets from beyond the ice line to explain the presence of close-in super-earths around M stars. In this scenario, the planet’s mass and occurrence rate at short orbits are determined by the disk properties at larger distances from the star. Owing to their figure 6, isolation masses similar to Kepler planets are reached outside of $\sim 10$ au. The isolation mass, $M_{\text{ISO}}$, scales with stellar mass, surface density, and distance from the star, $a$, as $M_{\text{ISO}} \propto M_\star^{1/2} \Sigma^{3/2} a^3$. The planet’s Hill sphere, a measure of the separation between planets, scales as $R_H \propto a \sqrt{M_{\text{ISO}}/M_\star}$. Factoring in a linear scaling between surface density and stellar mass based on millimeter-wave observations, the planet mass at fixed distance from the star scales with stellar mass as $M_{\text{ISO}} \propto M_\star$. The Hill sphere is independent of stellar mass, and the same number of isolation masses are formed. This model therefore predicts the same number of planets for low-mass stars, but smaller in size. This prediction is similar to that of the in-situ formation models, and is inconsistent with the increased planet occurrence towards lower mass stars and the lack of a strong trend in the planet radius distribution function with stellar mass.

### 4.3. Fewer binary companions around later spectral types

If binary companions inhibit planet formation, a lower binarity fraction towards later spectral type could explain the rising trend in planet occurrence. Mulders et al. (2015) discussed the impact of binaries on planet formation in the context of in situ formation, but found the effects to be insufficient to explain the trend in occurrence rate. If close-in planets form from material further out in the disk and migrated to their current locations, the possible disruptive impact of a binary companion is larger. Non-redundant aperture mask imaging of Kepler planet hosts show that they indeed lack short period (<50 au) binary companions, suggesting that planet formation is indeed inhibited by the presence of these companions (Kraus et al., ApJ Submitted).

Binaries with separations less than 50 au represent a significant fraction of the field star population. According to Raghavan et al. (2010), 50% of G stars and 35% of M stars have binary companions, of which approximately half interior to 50 au. Assuming a 100% planet formation efficiency for wider binaries, planet occurrence rate could increase by a factor $(1-0.175)/(1-0.25) = 1.1$ around M dwarfs, i.e. nowhere close to the factor 3.5 difference in planet occurrence rate. Even in the extreme case where binary companions would inhibit planet formation at all separations, the planet occurrence rate around M dwarfs would only increase by a factor of 1.3 with respect to that around G stars and could only partly explain the factor of 3.5 that is observed.

### 4.4. Fewer long-period giant planets around M dwarfs

Izidoro et al. (2015) proposed that giant planets formed at the snow line act as dynamical barriers to inward migrating super-earths and mini-Neptunes. Hence, the occurrence rates derived in this paper would be anticorrelated with those of long period giants. A similar correlation would be expected if subsequent inward and outward migration of giant planets destroys close-in super-Earths (Batygin & Laughlin 2015). In the core accretion model, low-mass disks around low-mass stars would be less likely to form giant planets (e.g. Laughlin et al. 2004), which might explain the overabundance of super-Earths around low-mass stars. Johnson et al. (2010) find that the occurrence rate of giant planets increases roughly linear with stellar mass, from 3% in M stars, $\sim 8.5\%$ in FGK stars, to 14% around A stars. These percentages are not high enough to explain the observed trend in Kepler planet occurrence, but it should be noted that current radial velocity surveys probe a limited range in baselines (3-10 years) and are likely incomplete in planet mass at longer periods. More complete estimates of the giant planet fraction find $f_M \sim 15\%$ for M stars including RV trends, (Montet et al. 2014) and $f_20 \sim 20\%$ for the population down to Saturn sizes and out to 20 au (Cumming et al. 2008).

The required giant planet fractions to explain the trend in Kepler occurrence rates are much higher. A giant
planet occurrence of $f_G \sim 70\%$ around G stars (and corresponding $f_M \sim 30\%$ in M stars) is necessary to reach $(1 - f_M)/(1 - f_G) \approx 2$. These numbers should be seen as lower limits, as giant planets may not stop all inward-migrating super-earths (Izidoro et al. 2015). Hence, the presence of long-period giants may only explain part of the increase in planet occurrence rates towards lower stellar masses.

4.5. Efficient redistribution of heavy-elements

If large-scale inward migration of solid material is more effective towards low-mass stars, an even larger population of planets must be present around higher mass stars at larger distances. Kepler only probes the planet population inside of roughly an au, while radial velocity surveys that probe larger distances from the star are mostly sensitive to giant planets. If smaller planets are sequestered at radii larger than ~1 au, they would escape detection in both samples. Micro-lensing surveys indicate that a population of super-earths ($5 - 10 M_\oplus$) and Neptunes ($10 - 30 M_\oplus$) are present around approximately half the (MGK) stars in the galaxy between 0.5 – 10 au (Cassan et al. 2012). This population presents a comparable amount of (heavy-element) mass in planetary systems as the Kepler planet population. There is no information on the stellar-mass dependence of this population, as most host stars remain unidentified. If the average planet mass and occurrence of this population correlates positively with stellar mass, it could represent the missing planet mass not seen at short orbits by Kepler. However, the planet mass and occurrence from micro-lensing surveys are estimated assuming no such scaling with stellar mass, and a stellar-mass dependency will alter the estimated planet mass and occurrence rates of this population.

There are two very efficient mechanisms for inward migration: radial drift of dust grains (Weidenschilling 1977), and type-I migration of (proto)planets (e.g. Goldreich & Tremaine 1979) [Lin & Papaloizou 1979]. If either of these mechanisms is responsible for increasing the heavy-element mass in the inner regions to create the population of super-earths and mini-Neptunes at short orbital periods, a stellar-mass dependency in the efficiency of this mechanism could explain the trends identified in this work. The efficiency of the first mechanism, radial drift of dust grains, was explored by Pinilla et al. (2013). The authors simulated the growth and drift of dust grains in brown dwarf disks, and find that radial drift is more efficient towards low-mass stars. If these inward drifting solids can be maintained in the inner disk by growing them into larger objects that stop drifting, for example by enhanced sticking (Boley et al. 2014), gravitational collapse (Chatterjee & Tan 2014, 2015), or pebble accretion onto pre-existing cores (Lambrechts & Johansen 2012) [Morbidelli et al. 2015], such a scenario would lead to an increased amount of heavy elements in the inner disk available for planet formation in low-mass stars. This mechanism would also deliver large amounts of volatiles to the inner disk when inward migrating solids cross the snow line and sublimate. It is not clear if this is consistent with the lack of observed water vapor in low-mass stars (Pascucci et al. 2013).

The efficiency of the other mechanism, type-I migration, can be estimated from the planet migration time-scale and the extent to which planets are trapped at short orbital periods. According to Eq. 70 from Tanaka et al. (2002) the planet migration time-scale, $\tau$ scales with stellar mass, disk temperature, $T$ and surface density as: $\tau \propto M_s^{1/2} \Sigma T$. Assuming a disk temperature of $T \propto r_P^{1/4} \propto M_s^{1/2}$ during the pre-main sequence and a surface density proportional to stellar mass yields a migration time-scale, $\tau \propto M_s^{1/2}$, i.e. independent of stellar mass. Hence it is not clear why migration of planetary building blocks would be more efficient around low-mass stars. Alternatively, lower-mass stars may be more efficient in halting migrating proto-planets at short orbital periods. Planet migration traps are a crucial ingredient in planet migration theories (e.g. Ida & Lin 2010). The inner edge of the gas disk presents a powerful planet trap (e.g. Masset et al. 2006), and our previous results indicate that the location of this trap is stellar-mass dependent (Mulders et al. 2015). The results of the current paper indicate that also the efficiency of this trap may be stellar-mass dependent. Planet traps also exists further out in the disk, associated with heat and surface density transitions in the disk (e.g. Hasegawa & Pudritz 2012). The relative importance of these traps changes with stellar mass, and may result in more close-in planets around low-mass stars (Hasegawa & Pudritz 2013).

4.6. A higher planet formation efficiency

The higher occurrence rate for close-in planets may simply point to a higher planet formation efficiency around lower mass stars, as also suggested by Muirhead et al. (2015) based on the high occurrence of compact multiples around mid-M dwarfs. Why lower-mass stars would be more efficient in converting their solid mass into planetary systems remains an open question. Perhaps the higher planet occurrence may be linked to longer disk lifetimes around low-mass stars (e.g. Carpenter et al. 2005) [Luhman & Mamajek 2012], allowing for more time for planets to form or migrate.

5. CONCLUSION

We derive the planet radius distribution for main-sequence stars of spectral types M to F probed by the Kepler spacecraft, and make an inventory of the average heavy-element mass locked up in planetary systems at short orbital periods. We find that:

- The average number of small planets ($1.0 - 2.8 R_\oplus$) per M star is a factor 3.5 higher than that per FGK star at orbital periods $P < 50$ days. The number of larger planets (“Neptunes”) is factor of 2 lower. Aside from the lack of Neptunes around M stars, there is no systematic trend in the planet radius distribution between F, G, and K stars that points to smaller planets forming around lower-mass stars.

- Taking into account the observed mass-radius relation for exoplanets, we show that higher occurrence rates around M stars are not the result of a redistribution of the same heavy-element mass into more numerous, smaller planets. M stars have, on average, a larger amount of heavy-element mass locked up in planetary systems at short orbital periods than FGK stars.
The majority of the heavy-element mass in short-period planets around FGK stars is locked up into mini-Neptunes ($1.5 - 4.0 \, R_{\oplus}$, $\sim 70\%$), with smaller fractions in rocky planets ($< 1.5 \, R_{\oplus}$, $\sim 10\%$) and Neptunes ($> 4 \, R_{\oplus}$, $\sim 10\%$). In M stars planetary systems, close to 100% of the (heavy-element) mass is located in planets smaller than $4 \, R_{\oplus}$, with $\sim 20\%$ in rocky planets smaller than $1.5 \, R_{\oplus}$.

Planets below the detection limit do not constitute a significant amount of (heavy-element) mass for $P < 50$ days, and Kepler has detected the bulk of the planet (heavy-element) mass out to 150 day orbital periods. In the region where Kepler is complete for all spectral types, the average heavy-element mass in planetary systems increases from $3.6 \pm 0.1 \, M_{\oplus}$ in F stars to $5.0 \pm 0.1 \, M_{\oplus}$ in G stars, $5.4 \pm 0.2 \, M_{\oplus}$ in K stars, and $7.3 \, M_{\oplus} \pm 0.7$ in M stars.

The roughly linear anticorrelation between heavy-element mass in planetary systems and stellar mass contrasts with the observed linear correlation between disk mass and stellar mass. This feature is currently not predicted by planet formation theories, either in situ or by migration. Such a feature may be explained by enhanced radial drift of solids of more efficient type-I migration of planetary building blocks towards lower-mass stars.

Acknowledgments:
This paper includes data collected by the Kepler mission. Funding for the Kepler mission is provided by the NASA Science Mission directorate. We thank the referee for the careful and constructive review. We would like to thank Fred Ciesla for providing comments on the manuscript, and Jessie Christiansen and Adam Kraus for sharing preprints of their papers. We would also like to thank Dean Billheimer and his students for statistical advice through the Statistical Consulting course. This material is based upon work supported by the National Aeronautics and Space Administration under Agreement No. NNX15AD94G for the program Earths in Other Solar Systems. The results reported herein benefited from collaborations and/or information exchange within NASAs Nexus for Exoplanet System Science (NExSS) research coordination network sponsored by NASAs Science Mission Directorate.

APPENDIX
A. COMPLETENESS PER SPECTRAL TYPE

Figure 9 shows the distribution of KOIs for spectral type sub-sample M to F. The region where Kepler is complete, indicated in blue, is limited by the completeness of the M star sample, which has the lowest number of stars. The red contour indicates the location where the expected detection frequency is one per bin for an occurrence rate of 10%, which is equivalent to an occurrence rate of 3 per logarithmic area unit. The lower limit of $0.5 \, R_{\oplus}$ is chosen because there are very few detection below. The M star sample limits the completeness to $P < 150$ days, $R_P < 16 \, R_{\oplus}$, and excludes a wedge from $(P, R_P) = (15, 0.7)$ to $(150, 1.4)$. We place the inner edge at an orbital period of 0.7 days. As shown in Figures 4 and 6, the excluded planets in the wedge contains at most 10% of the heavy-element mass at those orbital periods because they are smaller than $< 1.5 \, R_{\oplus}$. Varying the inner, lower, and upper boundary changes the total mass by only a few percent, and we have verified that this does not significantly change the trends with spectral type.

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Figure 9. Completeness limit overlaid on the KOI distribution for spectral type sub-samples M (top left), K (top right), G (bottom left), and F (bottom right). The red contour in the M star panel indicates the location out to which an occurrence rate of 10% can be detected.

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